- A two - port network is an electrical network with two separate ports for input and output.
- It has two terminal pairs acting as access points. The current entering one terminal of a pair leaves the other terminal in the pair.


Two - port network

- From the network, we can observe that there are 4 variables that is $I_{1}, I_{2}, V_{1}$ and $V_{2}$, which two are independent.
- The various term that relate these voltages and currents are called parameters.


## Z - PARAMETER

- Z - parameter also called as impedance parameter and the units is ohm ( $\Omega$ )
- Impedance parameters is commonly used in the synthesis of filters and also useful in the design and analysis of impedance matching networks and power distribution networks.
- The two - port network may be voltage - driven or current - driven.
- Two - port network driven by voltage source.

- Two - port network driven by current sources.

- The "black box" is replace with Z-parameter is as shown below.

- The terminal voltage can be related to the terminal current as:

$$
\begin{align*}
& V_{1}=z_{11} I_{1}+z_{12} I_{2}  \tag{1}\\
& V_{2}=z_{21} I_{1}+z_{22} I_{2} \tag{2}
\end{align*}
$$

- In matrix form as:

$$
\left[\begin{array}{l}
V_{1} \\
V_{2}
\end{array}\right]=\left[\begin{array}{ll}
z_{11} & z_{12} \\
z_{21} & z_{22}
\end{array}\right]\left[\begin{array}{l}
I_{1} \\
I_{2}
\end{array}\right]
$$

- The Z-parameter that we want to determine are $z_{11}$, $\mathrm{z}_{12}, \mathrm{z}_{21}, \mathrm{z}_{22}$.
- The value of the parameters can be evaluated by setting:

1. $I_{1}=0$ (input port open - circuited)
2. $I_{2}=0$ (output port open - circuited)

- Thus,

$$
\begin{array}{ll}
z_{11}=\left.\frac{V_{1}}{I_{1}}\right|_{I_{2}=0} & z_{12}=\left.\frac{V_{1}}{I_{2}}\right|_{I_{1}=0} \\
z_{21}=\left.\frac{V_{2}}{I_{1}}\right|_{I_{2}=0} & z_{22}=\left.\frac{V_{2}}{I_{2}}\right|_{I_{1}=0}
\end{array}
$$

- Where;
$\mathrm{z}_{11}=$ open - circuit input impedance.
$z_{12}=$ open - circuit transfer impedance from port 1 to port 2.
$z_{21}=$ open - circuit transfer impedance from port 2
to port 1.
$z_{22}=$ open - circuit output impedance.


## Example 1

Find the Z - parameter of the circuit below.


